

Statistical tests

Abhijit Dasgupta

BIOF 339

Comparing two groups

The t-test

The t-test compares whether the mean of a variable differs between two groups.

It does assume the normal distribution for the data, but is robust to deviations from normality

Do **not** test for normality before doing the t-test. It isn't necessary and screws up your error rates

The t-test

In R, there is a convenient function `t.test`

```
t.test(NP_958782 ~ ER.Status, data = brca)
```

```
Welch Two Sample t-test

data:  NP_958782 by ER.Status
t = 0.63522, df = 41.807, p-value = 0.5287
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -0.3523151  0.6759226
sample estimates:
mean in group Negative mean in group Positive
      0.4292798           0.2674761
```

Read the code as

"Do a t-test to see if (the mean of) `NP_958782` differs by `ER.Status`, where both are taken from the data set `brca`"

You can read the `~` as "by", as in "t-test of `NP_958782` by `ER.Status`"

Using broom

The fact that `broom::tidy` makes the results of tests into tibbles is in fact extremely useful in high-throughput work

```
brca %>%
  select(ER.Status, starts_with('NP')) %>%
  pivot_longer(names_to = 'protein',
               values_to = 'expression',
               cols = c(-ER.Status)) %>%
  split(.$protein) %>%
  map(~broom::tidy(t.test(expression ~ ER.Status,
                          data=..))) %>%
  bind_rows(.id = 'Protein') %>%
  select(Protein, estimate, p.value, conf.low, conf.high)
```

```
# A tibble: 10 × 5
  Protein estimate p.value conf.low co
  <chr>      <dbl>   <dbl>   <dbl>
1 NP_000436  0.161 0.534   -0.356
2 NP_001611 -1.41 0.000199 -2.10
3 NP_112598  0.160 0.761   -0.892
4 NP_958780  0.163 0.528   -0.354
5 NP_958781  0.162 0.530   -0.356
6 NP_958782  0.162 0.529   -0.352
7 NP_958783  0.164 0.527   -0.354
8 NP_958784  0.164 0.527   -0.354
9 NP_958785  0.165 0.524   -0.353
10 NP_958786  0.166 0.520   -0.351
```

Back to testing

Wilcoxon test, nonparametric t-test

```
wilcox.test(NP_958782 ~ ER.Status, data=brca) %>%  
  broom::tidy()
```

```
# A tibble: 1 × 4  
  statistic p.value method alternative  
  <dbl>    <dbl> <chr>      <chr>  
1      755  0.590 Wilcoxon rank sum test with continuity correction two.sided
```

Wilcoxon rank sum test with continuity correction

```
data: NP_958782 by ER.Status  
W = 755, p-value = 0.5897  
alternative hypothesis: true location shift is not equal to 0
```


Wilcoxon test

```
brca %>%
  select(ER.Status, starts_with('NP')) %>%
  tidyr::gather(protein, expression, -ER.Status) %>%
  split(.$protein) %>%
  map(~broom::tidy(wilcox.test(expression ~ ER.Status,
                              data=))) %>%
  bind_rows(.id='Protein') %>%
  select(Protein, p.value)
```

```
# A tibble: 10 × 2
  Protein      p.value
  <chr>        <dbl>
1 NP_000436  0.583
2 NP_001611  0.0000928
3 NP_112598  0.939
4 NP_958780  0.583
5 NP_958781  0.576
6 NP_958782  0.590
7 NP_958783  0.583
8 NP_958784  0.576
9 NP_958785  0.576
10 NP_958786  0.576
```

Using tableone

```
CreateTableOne(  
  data = brca %>% filter(!is.na(ER.Status)),  
  vars = brca %>%  
    select(starts_with('NP')) %>%  
    names(),  
  strata = 'ER.Status',  
  test = T,  
  testNormal = t.test  
)
```

		Stratified by ER.Status			
		Negative	Positive	p	test
n		38	69		
NP_958782	(mean (SD))	0.43 (1.13)	0.27 (0.93)	0.498	
NP_958785	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.492	
NP_958786	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.487	
NP_000436	(mean (SD))	0.43 (1.14)	0.27 (0.93)	0.502	
NP_958781	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.499	
NP_958780	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.496	
NP_958783	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.495	
NP_958784	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.495	
NP_112598	(mean (SD))	-0.20 (2.28)	-0.36 (1.97)	0.748	
NP_001611	(mean (SD))	-0.57 (1.54)	0.84 (1.19)	<0.001	

This is not quite the same results as before

Using tableone

```
CreateTableOne(  
  data = brca %>% filter(!is.na(ER.Status)),  
  vars = brca %>%  
    select(starts_with('NP')) %>%  
    names(),  
  strata = 'ER.Status',  
  test = T,  
  testNormal = t.test,  
  argsNormal = list(var.equal=F)  
)
```

	Stratified by		ER.Status		
		Negative	Positive	p	test
n		38	69		
NP_958782	(mean (SD))	0.43 (1.13)	0.27 (0.93)	0.529	
NP_958785	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.524	
NP_958786	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.520	
NP_000436	(mean (SD))	0.43 (1.14)	0.27 (0.93)	0.534	
NP_958781	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.530	
NP_958780	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.528	
NP_958783	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.527	
NP_958784	(mean (SD))	0.44 (1.14)	0.27 (0.93)	0.527	
NP_112598	(mean (SD))	-0.20 (2.28)	-0.36 (1.97)	0.761	
NP_001611	(mean (SD))	-0.57 (1.54)	0.84 (1.19)	<0.001	

Tests for discrete data

Testing whether the distribution of a categorical variable differs by levels of another categorical variable can be done using either the Chi-square test (`chisq.test`) or the Fisher's test (`fisher.test`). Both require you to create a 2x2 table first.

```
fisher.test(table(brca$Tumor, brca$ER.Status))
```

```
Fisher's Exact Test for Count Data
```

```
data: table(brca$Tumor, brca$ER.Status)
p-value = 0.6003
alternative hypothesis: two.sided
```

Tests for discrete data

Testing whether the distribution of a categorical variable differs by levels of another categorical variable can be done using either the Chi-square test (`chisq.test`) or the Fisher's test (`fisher.test`). Both require you to create a 2x2 table first.

```
chisq.test(table(brca$Tumor, brca$ER.Status))
```

```
Pearson's Chi-squared test
```

```
data: table(brca$Tumor, brca$ER.Status)  
X-squared = 2.094, df = 3, p-value = 0.5531
```

Tests for discrete data

We can use `broom::tidy` for either of these

```
chisq.test(table(brca$Tumor, brca$ER.Status)) %>%  
  broom::tidy()
```

```
# A tibble: 1 × 4  
  statistic p.value parameter method  
  <dbl>    <dbl>    <int> <chr>  
1      2.09  0.553         3 Pearson's Chi-squared test
```

Using tableone

```
CreateCatTable(vars = c('Tumor', 'Node', 'Metastasis'),  
              data = filter(brca, !is.na(ER.Status)),  
              strata = 'ER.Status',  
              test = T) # chisq.test
```

	Stratified by ER.Status			
n	Negative	Positive	p	test
Tumor (%)	38	69		
T1	6 (15.8)	10 (14.5)		0.553
T2	26 (68.4)	40 (58.0)		
T3	5 (13.2)	14 (20.3)		
T4	1 (2.6)	5 (7.2)		
Node (%)				0.685
N0	22 (57.9)	32 (46.4)		
N1	8 (21.1)	21 (30.4)		
N2	5 (13.2)	10 (14.5)		
N3	3 (7.9)	6 (8.7)		
Metastasis = M1 (%)	1 (2.6)	1 (1.4)		1.000

Using tableone

```
c1 <- CreateCatTable(vars = c('Tumor', 'Node', 'Metastasis'),  
  data = filter(brca, !is.na(ER.Status)),  
  strata = 'ER.Status',  
  test = T)  
print(c1, exact = c('Tumor', 'Node', 'Metastasis')) # fisher.test
```

	Stratified by ER.Status			
n	Negative	Positive	p	test
Tumor (%)	38	69		
T1	6 (15.8)	10 (14.5)		
T2	26 (68.4)	40 (58.0)		
T3	5 (13.2)	14 (20.3)		
T4	1 (2.6)	5 (7.2)		
Node (%)			0.695	exact
N0	22 (57.9)	32 (46.4)		
N1	8 (21.1)	21 (30.4)		
N2	5 (13.2)	10 (14.5)		
N3	3 (7.9)	6 (8.7)		
Metastasis = M1 (%)	1 (2.6)	1 (1.4)	1.000	exact